# Package 'irtoys'

July 2, 2014

Type Package

**Title** Simple interface to the estimation and plotting of IRT models

Version 0.1.7

Date 2014-01-20

Author Ivailo Partchev

**Description** Provides a simple common interface to the estimation of item parameters in IRT models for binary responses with three different programs (ICL, BILOG-MG, and ltm, and a variety of functions useful with IRT models.

LazyLoad yes

LazyData yes

**License** GPL (>= 2)

Depends sm, ltm

Suggests MASS

**Collate** 'ability.R' 'estimate.R' 'itemfit.R' 'nonpar.R' 'readin.R' 'scale.R' 'tracelines.R' 'utils.R' 'irtoys-package.R'

NeedsCompilation no

Repository CRAN

**Date/Publication** 2014-01-23 00:16:27

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## $\mathsf{R}$ topics documented:

dpv       :eap         est       :iif         iif       !if         iif       !if         mlebme       !a         normal.qu       !a         npp       !a         plot.iif       !a         plot.tif       !a         plot.trf       !a         qrs       2         read.ip.bilog       2         read.ip.icl       2         read.qu.icl       2         read.resp       2         sca       2         sco       2         Scored       2         sco       2         scp       2         sim       2         tet       2         tgp       2         tia       3         tif       3         trf       3         tsc       3         Unscored       3         wle       3	irtoys-package	 		 			 	•	 						2
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irtoys-package

Estimate and plot IRT models for binary responses

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#### **Description**

Package: irtoys
Type: Package
Version: 0.1.4
Date: 2011-06-22

License: GPL (>= 2)

LazyLoad: yes LazyData: yes

#### **Details**

Provides a common interface to the estimation of item parameters in IRT models for binary responses with three different programs (ICL, BILOG, and 1tm, and a variety of functions useful with IRT models.

The irtoys package contains a bunch of functions potentially useful to those teaching or learning Item Response Theory (IRT). Although there is no shortage of good IRT programs, those tend to have wildly different and often unwieldy user interfaces. Besides, no single program does everything one needs. Item parameters can be estimated with a program like ICL or BILOG, non-parametric approaches are implemented in TestGraf, transformation to a common scale needs ST, and so on. Some programs, such as ICL, have no graphical capabilities at all, while others offer stunning interactive graphics but refuse to output a Postscript file.

Package irroys provides a common interface to some of the most basic functions in ICL, BILOG, and 's own 1tm, some of the functionality of TestGraf and ST, and a variety of other functions. Those who want to take advantage of the full functionality of ICL, BILOG & Co. must still master their syntax.

To take full advantage of irtoys, some IRT software is needed. Package 1tm is automatically loaded. ICL by Brad Hanson can be downloaded from his site, www.b-a-h.com: executables are provided for Windows, Linux, and Macintosh. BILOG is commercial software sold by SSI — see www.ssicentral.com for further detail.

On Windows, make sure that the executable files (icl.exe for ICL, BLM1.EXE, BLM2.EXE, and BLM3.EXE for BILOG) are located in a directory that is included in the PATH variable. On Linux, BILOG, being a Windows program, is run with wine, and should also be on a path where wine can find it. On my machine, I have simply put the three files in ~/.wine/drive\_c/windows/. It seems that new versions of wine expect them to be explicitly tagged as executable. On Macintosh, at least 1tm should work in all cases.

NOTE: Starting with version 0.1.6, function est returns a list of two matrices: est contains the parameter estimates and is thus identical to the output in earlier versions, and se contains the standard errors, in a similar format. Also, function itf now returns item fit statistics as a vector rather than a list. Finally, since most of the functions in irtoys have been written with the "logistic" metric in mind (i.e.,  $a_j(\theta_i - b_j)$  rather than  $1.7a_j^*(\theta_i - b_j)$ , function est now estimates item parameters only in the logistic metric.

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#### Author(s)

Ivailo Partchev <partchev@gmail.com>

#### References

S. E. Embretson and S. P. Reise (2000), Item Response Theory for Psychologists, Lawrence Erlbaum Associates, Mahwah, NJ

api

The Z3 appropriateness index

#### **Description**

Computes the Z3 appropriateness index, a measure of person fit in IRT models

## Usage

```
api(resp, ip, theta)
```

## Arguments

resp	A matrix of responses: persons as rows, items as columns, entries are either 0 or 1, no missing data
ip	Item parameters: a matrix with one row per item, and three columns: [,1] item discrimination $a$ , [,2] item difficulty $b$ , and [,3] asymptote $c$ .
theta	A measure of ability, typically produced with mlebme, wle etc. If missing, ML estimates will be computed automatically.

## Value

A vector of length equal to the number of rows in resp, containing the appropriateness indices

#### Author(s)

Ivailo Partchev

## References

Drasgow, F., Levine, M. V., & Williams, E. A. (1985). Appropriateness measurement with polychotomous item response models and standardized indices. British Journal of Mathematical and Statistical Psychology, 38, 67–80

```
api(Scored, Scored2pl$est)
```

dpv 5

dpv	Draw plausible values	

## Description

Draws (by rejection sampling) plausible values from the posterior distribution of ability

## Usage

```
dpv(resp, ip, mu = 0, sigma = 1, n = 5)
```

## Arguments

resp	A matrix of responses: persons as rows, items as columns, entries are either 0 or 1, no missing data
ip	Item parameters: a matrix with one row per item, and three columns: [,1] item discrimination $a$ , [,2] item difficulty $b$ , and [,3] asymptote $c$ .
mu	Mean of the apriori distribution. Ignored when method="ML". Default is 0.
sigma	Standard deviation of the apriori distribution. Ignored when $\mbox{method="ML"}$ . Default is 1.
n	The number of plausible values to draw for each person (default is 5).

## Value

A matrix with n columns

## Author(s)

Ivailo Partchev

## See Also

```
mlebme, eap
```

```
plval <- dpv(resp=Scored, ip=Scored2pl$est)</pre>
```

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eap
-----

EAP estimation of ability

## Description

Estimates the expectation of the posterior distribution of the latent variable ("ability") for each person.

## Usage

```
eap(resp, ip, qu)
```

## Arguments

resp	A matrix of responses: persons as rows, items as columns, entries are either $0$ or $1$ , no missing data
ip	Item parameters: a matrix with one row per item, and three columns: [,1] item discrimination $a$ , [,2] item difficulty $b$ , and [,3] asymptote $c$ .
qu	A quadrature object produced with normal.qu or read in with read.qu.icl

## Value

A matrix with the ability estimates in column 1, and their standard errors of measurement (SEM) in column 2, and the number of non-missing reponses in column 3

## Author(s)

Ivailo Partchev

## See Also

```
mlebme, normal.qu, read.qu.icl
```

```
th.eap <- eap(resp=Scored, ip=Scored2pl$est, qu=normal.qu())</pre>
```

est 7

est	Estimate item parameters
-----	--------------------------

## Description

Estimate IRT item parameters using either ICL, BILOG, or 1tm. Provides access to the most widely used options in these programs.

## Usage

```
est(resp, model = "2PL", engine = "icl", nqp = 20,
  est.distr = FALSE, nch = 5, a.prior = TRUE,
b.prior = FALSE, c.prior = TRUE, bilog.defaults = TRUE,
  rasch = FALSE, run.name = "mymodel")
```

## Arguments

resp	A matrix of responses: persons as rows, items as columns, entries are either 0 or 1, no missing data
model	The IRT model: "1PL", "2PL", or "3PL". Default is "2PL".
engine	One of "icl", "bilog", or "ltm". Default is "icl".
nqp	Number of quadrature points. Default is 20.
est.distr	T if the probabilities of the latent distribution are to be estimated, F if a normal distribution is assumed. Default is F. Ignored when ${\sf engine="ltm"}$ .
nch	Number of choices in the original item formulation. Used to determine the prior for the asymptote when engine="bilog", model="3PL", and c.prior=T. Default is $5$ .
a.prior	Whether a prior for the item discriminations is used. Ignored when $model="1PL"$ or engine="ltm". Default is T.
b.prior	Whether a prior for the item difficulties is used. Ignored when engine="ltm". Default is F.
c.prior	Whether a prior for the asymptotes is used. Ignored when $model="1PL"$ or $model="2PL"$ or $engine="ltm"$ . Default is T.
bilog.defaults	When engine="icl" and a prior is used, use the default priors in BILOG rather than the default priors in ICL. Ignored when engine="ltm". Default is T.
rasch	When engine="bilog" and model="1PL" and "rasch"=T, the common value for discriminations is forced to 1, and the sum of the difficulties is 0. When engine="ltm" and model="1PL" and "rasch"=T, the common value for discriminations is forced to 1. Ignored in all other cases. Default is F.
run.name	A (short) string used in the names of all files read or written by ICL or BILOG. Default is "mymodel". Change to something else to keep the outputs of ICL of BILOG for further use. Ignored when engine="ltm"

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#### **Details**

Estimate the parameters of an IRT model defined in the most general case ("3PL") as

$$P(U_{ij} = 1 | \theta_i, a_j, b_j, c_j) = c_j + (1 - c_j) \frac{\exp(a_j(\theta_i - b_j))}{1 + \exp(a_j(\theta_i - b_j))}$$

where  $U_{ij}$  is a binary response given by person i to item j,  $\theta_i$  is the value of the latent variable ("ability") for person i,  $a_j$  is the discrimination parameter for item j,  $b_j$  is the difficulty parameter for item j,  $c_j$  is the asymptote for item j.

Some authors prefer to represent the model with a logit  $1.7a_j^*(\theta_i - b_j)$  rather than  $a_j(\theta_i - b_j)$ . This option has been removed from irroys as it is not supported by the remaining functions of the package.

In the 2PL model (model="2PL"), all asymptotes  $c_j$  are 0. In the 1PL model (model="1PL"), all asymptotes  $c_j$  are 0 and the discriminations  $a_j$  are equal for all items (and sometimes to 1).

Package irtoys provides a simple common interface to the estimation of item parameters with three different programs. It only accesses the most basic and widely used options in these programs. Each of the three programs has a much wider choice of options and cababilities, and serious users must still learn the corresponding syntax in order to access the advanced features. Even when models are fit "by hand", irtoys may be useful in plotting results, doing comparisons across programs etc.

Estimation of the more complex IRT models (2PL and 3PL) for some "difficult" data sets often has to use prior distributions for the item parameters. irtoys adopts the default behaviour of BILOG: no priors for b in any model, priors for a in the 2PL and 3PL models, priors for c in the 3PL model. This can be overriden by changing the values of a prior, b prior, and c prior.

If priors are used at all, they will be the same for all items. Note that both ICL and BILOG can, at some additional effort, set different priors for any individual item. At default, the common priors are the BILOG defaults: normal (0, 2) for b, lognormal (0, 0.5) for a, and beta(20\*p+1, 20(1-p)+1) for c; p is 1 over the number of choices in the original item formulations, which can be set with the parameter nch, and is again assumed the same for all items.

When engine="icl" and bilog.defaults=F, any priors used will be the ICL default ones, and based on the 4-parameter beta distribution: beta(1.01, 1.01, -6, 6) for b, beta(1.75, 3, 0, 3) for a, and beta(3.5, 4, 0, 0.5) for c. When engine="ltm", all commands involving priors are ignored.

est only works when some IRT software is installed. Package 1tm is automatically loaded. ICL can be downloaded from www.b-a-h.com. BILOG is commercial software sold by SSI — see www.ssicentral.com for further detail. On Windows, make sure that the executable files (icl.exe for ICL, blm1.exe, blm2.exe, and blm3.exe, for BILOG) are located in directories that are included in the PATH variable.

#### Value

A list with two elements, est and se, for the parameter estimates and their standard errors, correspondingly. Each element is a matrix with one row per item, and three columns: [,1] item discrimination a, [,2] item difficulty b, and [,3] asymptote c. For the 1PL and 2PL models, all asymptotes are equal to 0; for the 1PL, the discriminations are all equal but not necessarily equal to 1. When ICL is used as estimation engine, se is NULL as ICL does not compute standard errors for the item parameter estimates.

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#### Author(s)

Ivailo Partchev

#### References

Bradley A. Hanson (2002), ICL: IRT Command Language. www.b-a-h.com

Dimitris Rizopoulos (2006). ltm: Latent Trait Models under IRT. cran.r-project.org

M. F. Zimowski, E. Muraki, R. J. Mislevy and R. D. Bock (1996), BILOG–MG. Multiple-Group IRT Analysis and Test Maintenance for Binary Items, SSI Scientific Software International, Chicago, IL. www.ssicentral.com

## **Examples**

```
p.1pl <- est(Scored, model="1PL", engine="1tm")
p.2pl <- est(Scored, model="2PL", engine="1tm")</pre>
```

iif

Item information function

## **Description**

The item information function (IIF) for the 3PL model can be computed as

$$I(\theta) = a^2 \frac{Q(\theta)}{P(\theta)} \left[ \frac{P(\theta) - c}{1 - c} \right]^2,$$

where  $\theta$  is the value of the latent variable for a person, a is the discrimination parameter for the item, P is the IRF for the person and item, and Q = 1 - P. For the 1PL and 2PL models, the expression reduces to  $a^2PQ$ .

#### Usage

```
iif(ip, x = NULL)
```

#### **Arguments**

Х

Item parameters: a matrix with one row per item, and three columns: [,1] item discrimination a, [,2] item difficulty b, and [,3] asymptote c.

The values of the latent variable ( $\theta$  in the equation above), at which the IIF will be evaluated. If not given, 99 values spaced evenly between -4 and +4 will be used, handy for plotting.

## **Details**

A common use of this function would be to obtain a plot of the IIF.

irf

#### Value

A list of:

x A copy of the argument x

f A matrix containing the IIF values: persons (values of (x) as rows and items as columns

#### Author(s)

Ivailo Partchev

#### See Also

```
plot.iif, irf
```

#### **Examples**

```
plot(iif(Scored2pl$est[1:3,]))
```

irf

Item response function

#### **Description**

Returns the item response function of the 3PL (1PL, 2PL) model, the i.e. the probabilities defined by

$$P(U_{ij} = 1 | \theta_i, a_j, b_j, c_j) = c_j + (1 - c_j) \frac{\exp(a_j(\theta_i - b_j))}{1 + \exp(a_j(\theta_i - b_j))}$$

where  $U_{ij}$  is a binary response given by person i to item j,  $\theta_i$  is the value of the latent variable ("ability") for person i,  $a_j$  is the discrimination parameter for item j,  $b_j$  is the difficulty parameter for item j,  $c_j$  is the asymptote for item j. Some authors call the IRF "the item characteristic curve".

## Usage

$$irf(ip, x = NULL)$$

## **Arguments**

Х

ip Item parameters: a matrix with one row per item, and three columns: [,1] item

discrimination a, [,2] item difficulty b, and [,3] asymptote c.

The values of the latent variable ( $\theta$  in the equation above), at which the IRF will be evaluated. If not given, 99 values spaced evenly between -4 and +4 will be used, handy for plotting.

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#### **Details**

In the 2PL model (model="2PL"), all asymptotes  $c_j$  are 0. In the 1PL model (model="1PL"), all asymptotes  $c_j$  are 0 and the discriminations  $a_j$  are equal for all items (and sometimes to 1).

A common use of this function would be to obtain a plot of the IRF.

#### Value

A list of:

x A copy of the argument x

f A matrix containing the IRF values: persons (values of (x) as rows and items as columns

#### Author(s)

Ivailo Partchev

#### See Also

```
plot.irf
```

## **Examples**

```
plot(irf(Scored2pl$est[1,]))
```

itf

Test item fit

#### **Description**

Returns a statistic of item fit together with its degrees of freedom and p-value. Optionally produces a plot.

## Usage

```
itf(resp, ip, item, stat = "lr", theta,
  standardize = TRUE, mu = 0, sigma = 1, bins = 9,
  breaks = NULL, equal = "count", type = "means",
  do.plot = TRUE, main = "Item fit")
```

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#### **Arguments**

resp	A matrix of responses: persons as rows, items as columns, entries are either 0 or 1, no missing data
ip	Item parameters: a matrix with one row per item, and three columns: [,1] item discrimination $a$ , [,2] item difficulty $b$ , and [,3] asymptote $c$ .
item	A single number pointing to the item (column of resp, row of ip), for which fit is to be tested
stat	The statistic to be computed, either "chi" or "lr". Default is "lr". See details below.
theta	A vector containing some viable estimate of the latent variable for the same persons whose responses are given in resp. If not given (and group is also missing), EAP estimates will be computed from resp and ip.
standardize	Standardize the distribution of ability estimates?
mu	Mean of the standardized distribution of ability estimates
mu sigma	Mean of the standardized distribution of ability estimates  Standard deviation of the standardized distribution of ability estimates
	·
sigma	Standard deviation of the standardized distribution of ability estimates
sigma bins	Standard deviation of the standardized distribution of ability estimates Desired number of bins (default is 9)
sigma bins breaks	Standard deviation of the standardized distribution of ability estimates  Desired number of bins (default is 9)  A vector of cutpoints. Overrides bins if present.  Either "width" for bins of equal width, or "count" for bins with roughly counts
sigma bins breaks equal	Standard deviation of the standardized distribution of ability estimates  Desired number of bins (default is 9)  A vector of cutpoints. Overrides bins if present.  Either "width" for bins of equal width, or "count" for bins with roughly counts of observations. Default is "quant"  The points at which itf will evaluate the IRF. One of "mids" (the mid-point of each bin), "meds" (the median of the values in the bin), or "means" (the mean

## **Details**

Given a long test, say 20 items or more, a large-test statistic of item fit could be constructed by dividing examinees into groups of similar ability, and comparing the observed proportion of correct answers in each group with the expected proportion under the proposed model. Different statistics have been proposed for this purpose.

The chi-squared statistic

$$X^{2} = \sum_{g} (N_{g} \frac{(p_{g} - \pi_{g})^{2}}{\pi_{g}(1 - \pi_{g})},$$

where  $N_g$  is the number of examinees in group  $g, p_g = r_g/N_g, r_g$  is the number of correct responses to the item in group g, and  $\pi_g$  is the IRF of the proposed model for the median ability in group g, is attributed by Embretson & Reise to R. D. Bock, although the article they cite does not actually mention it. The statistic is the sum of the squares of quantities that are often called "Pearson residuals" in the literature on categorical data analysis.

BILOG uses the likelihood-ratio statistic

$$X^{2} = 2\sum_{g} \left[ r_{g} \log \frac{p_{g}}{\pi_{g}} + (N_{g} - r_{g}) \log \frac{(1 - p_{g})}{(1 - \pi_{g})} \right],$$

itf 13

where  $\pi_q$  is now the IRF for the mean ability in group g, and all other symbols are as above.

Both statistics are assumed to follow the chi-squared distribution with degrees of freedom equal to the number of groups minus the number of parameters of the model (eg 2 in the case of the 2PL model). The first statistic is obtained in itf with stat="chi", and the second with stat="lr" (or not specifying stat at all).

In the real world we can only work with estimates of ability, not with ability itself. irtoys allows use of any suitable ability measure via the argument theta. If theta is not specified, itf will compute EAP estimates of ability, group them in 9 groups having approximately the same number of cases, and use the means of the ability eatimates in each group. This is the approximate behaviour of BILOG.

If the test has less than 20 items, itf will issue a warning. For tests of 10 items or less, BILOG has a special statistic of fit, which can be found in the BILOG output. Also of interest is the fit in 2- and 3-way marginal tables in package 1tm.

#### Value

A vector of three numbers:

Statistic The value of the statistic of item fit

DF The degrees of freedom

P-value The p-value

## Author(s)

Ivailo Partchev

## References

S. E. Embretson and S. P. Reise (2000), Item Response Theory for Psychologists, Lawrence Erlbaum Associates, Mahwah, NJ

M. F. Zimowski, E. Muraki, R. J. Mislevy and R. D. Bock (1996), BILOG–MG. Multiple-Group IRT Analysis and Test Maintenance for Binary Items, SSI Scientific Software International, Chicago, IL

#### See Also

```
eap, qrs
```

```
fit <- itf(resp=Scored, ip=Scored2pl$est, item=7)</pre>
```

14 mlebme

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Maximum likelihood and Bayes Modal estimation of ability

## Description

Estimates the value of the latent variable ("ability") for each person by direct optimization

## Usage

```
mlebme(resp, ip, mu = 0, sigma = 1, method = "ML")
```

## Arguments

resp	A matrix of responses: persons as rows, items as columns, entries are either 0 or 1, no missing data
ip	Item parameters: a matrix with one row per item, and three columns: [,1] item discrimination $a$ , [,2] item difficulty $b$ , and [,3] asymptote $c$ .
mu	Mean of the apriori distribution. Ignored when method="ML". Default is 0.
sigma	Standard deviation of the apriori distribution. Ignored when $method="ML"$ . Default is 1.
method	"ML" for maximum likelihood or "BM" for Bayes Modal estimation. Default is "ML", in which case any values for mu and sigma will be ignored.

## Value

A matrix with the ability estimates in column 1 and their standard errors of measurement (SEM) in column 2, and the number of non-missing responses in column 3

## Author(s)

Ivailo Partchev

## See Also

eap

```
th.mle <- mlebme(resp=Scored, ip=Scored2pl$est)</pre>
```

normal.qu 15

normal.qu Normal quadrature points and weights
--

## **Description**

Quadrature points and weights based on the Normal distribution. Quadrature objects are used when estimating abilities with eap and for some of the scaling methods in sca.

## Usage

```
normal.qu(n = 15, lower = -4, upper = 4, mu = 0,
   sigma = 1, scaling = "points")
```

## **Arguments**

n	Number of	of quadrature	points
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lower Lower boundary upper Upper boundary

mu Mean

sigma Standard deviation

scaling Determines the way in which non-default values of mu and sigma are applied.

When scaling="points", the quadrature points are rescaled, otherwise the

quadrature weights are adapted.

#### Value

A list of:

quad.points A vector of n quadrature points

quad.weights A vector of the corresponding quadrature weights

#### Author(s)

Ivailo Partchev

## See Also

```
read.qu.icl, eap, sca
```

```
quad <- normal.qu(n=20)</pre>
```

16 npp

npp	Non-parametric characteristic curves

## **Description**

A plotting routine producing non-parametric analogues of the IRF not unlike those in Jim Ramsay's TestGraf program. The curves are produced by a kernel binomial regression of the actual responses to an item on some estimates of the latent variable, by courtesy of package sm.

## Usage

```
npp(resp, x, items, from = -4, to = 4, co = 1,
  main = "Non-parametric response function", add = FALSE,
  bands = FALSE, label = FALSE)
```

## **Arguments**

resp	A matrix of responses: persons as rows, items as columns, entries are either 0 or
	1, no missing data
х	The values of the latent variable ("ability") for the same persons whose responses are given in resp. If not given, function qrs will be plugged in, which is the approach of TestGraf
items	An index to the items (columns of resp) to be shown on the plot. If not given, all items will be plotted.
from	Lower limit for ability on the plot. Default is -4.
to	Upper limit for ability on the plot. Default is 4.
add	When add=T, the curve is added to a plot, otherwise a new plot is started. Default is F.
main	The main title of the plot, given that add=F.
СО	The colour of the curves. Default is 1 for black. Use co=NA to plot each curve in a different colour.
bands	When bands=T, confidence bands are added.
label	When label=T, individual curves will be labeled with the item number.

## Author(s)

Ivailo Partchev

## References

James O. Ramsay (2000). TestGraf: A program for the graphical analysis of multiple choice test and questionnaire data. McGill University, Montreal, Canada

plot.iif

#### See Also

```
qrs, irf, plot.irf
```

## **Examples**

```
# plot items 1:5 in different colours, label
npp(Scored, items=1:5, co=NA, label=TRUE)

# For item 7, compare npp with the 2PL parametric IRF
npp(Scored, items=7, bands=TRUE)
plot(irf(ip=Scored2pl$est[7,]), co=3, add=TRUE)
```

plot.iif

A plot method for item information functions

## **Description**

Useful for plotting item information functions. The x argument of iif should better be left out unless something special is required.

## Usage

```
## S3 method for class 'iif'
plot(x, add = FALSE,
    main = "Item information function", co = 1,
    label = FALSE, ...)
```

#### **Arguments**

X	An object produced by function iif
add	When add=T, the IIF is added to a plot, otherwise a new plot is started. Default is $F$ .
main	The main title of the plot, given that add=F.
со	The colour of the IIF curve. Default is 1 for black. Use co=NA to plot each IIF in a different colour.
label	When label=T, individual curves will be labeled with the item number.
	Any additional plotting parameters

## Author(s)

Ivailo Partchev

#### See Also

iif

18 plot.irf

#### **Examples**

```
# plot IIF for all items in red, label with item number
plot(iif(Scored2pl$est), co="red", label=TRUE)
# plot IIF for items 2, 3, and 7 in different colours
plot(iif(Scored2pl$est[c(2,3,7),]), co=NA)
```

plot.irf

A plot method for item response functions

## **Description**

Useful for plotting item response functions. The x argument of irf should better be left out unless something special is required.

## Usage

```
## S3 method for class 'irf'
plot(x, add = FALSE,
    main = "Item response function", co = 1, label = FALSE,
    ...)
```

## Arguments

X	An object produced by function irf
add	When add=T, the IRF is added to a plot, otherwise a new plot is started. Default is F.
main	The main title of the plot, given that add=F.
СО	The colour of the IRF curve. Default is 1 for black. Use co=NA to plot each IRF in a different colour.
label	When label=T, individual curves will be labeled with the item number.
	Any additional plotting parameters

#### Author(s)

Ivailo Partchev

## See Also

irf

```
# plot IRF for all items in red, label with item number
plot(irf(Scored2pl$est), co="red", label=TRUE)
# plot IRF for items 2, 3, and 7 in different colours
plot(irf(Scored2pl$est[c(2,3,7),]), co=NA)
```

plot.tif

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A plot method for test information functions

## Description

Useful for plotting test information functions. The x argument of tif should better be left out unless something special is required.

## Usage

```
## S3 method for class 'tif'
plot(x, add = FALSE,
    main = "Test information function", co = 1, ...)
```

## Arguments

X	An object produced by function tif
add	When add=T, the TIF is added to a plot, otherwise a new plot is started. Default is F.
main	The main title of the plot, given that add=F.
со	The colour of the TIF curve. Default is 1 for black. Use co=NA to plot each TIF in a different colour.
	Any additional plotting parameters

## Author(s)

Ivailo Partchev

## See Also

tif

```
plot(tif(Scored2pl$est))
```

20 plot.trf

plot.trf	-			_
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A plot method for test response functions

## Description

Useful for plotting test response functions. The x argument of trf should better be left out unless something special is required.

## Usage

```
## S3 method for class 'trf'
plot(x, add = FALSE,
    main = "Test response function", co = 1, ...)
```

## Arguments

X	An object produced by function trf
add	When add=T, the IRF is added to a plot, otherwise a new plot is started. Default is F.
main	The main title of the plot, given that add=F.
со	The colour of the TRF curve. Default is 1 for black. Use co=NA to plot each TRF in a different colour.
	Any additional plotting parameters

## Author(s)

Ivailo Partchev

## See Also

trf

```
plot(trf(Scored2pl$est))
```

qrs 21

qrs

Quantiles of the ranked sum scores

## Description

A rough estimate of the values of the latent variable ("ability"). The sum scores (number of correct responses) are ranked, breaking ties at random. The ranks are divided by the sample size + 1, and the corresponding quantiles of the standard Normal distribution are returned. Used as default in the non-parametric IRF plots produced by npp in analogy to Jim Ramsay's TestGraf. Another possible use is in itf.

## Usage

```
qrs(resp)
```

## **Arguments**

resp

A matrix of responses: persons as rows, items as columns, entries are either 0 or 1, no missing data

#### Value

A one-column matrix of values

#### Author(s)

Ivailo Partchev

## See Also

```
npp, itf
```

#### **Examples**

```
sc <- qrs(Scored)</pre>
```

read.ip.bilog

Read in parameter estimates

## **Description**

From BILOG output, read in estimates of item parameters. Invoked automatically when the model is estimated via irroys. If that is not the case, file must be a file produced with the >SAVE PARm file; command in BILOG.

22 read.ip.icl

#### Usage

```
read.ip.bilog(file)
```

#### **Arguments**

file

File name

#### Value

A list with two elements, est and se, for the parameter estimates and their standard errors, correspondingly. Each element is a matrix with one row per item, and three columns: [,1] item discrimination a, [,2] item difficulty b, and [,3] asymptote c. For the 1PL and 2PL models, all asymptotes are equal to 0; for the 1PL, the discriminations are all equal but not necessarily equal to 1.

#### Author(s)

Ivailo Partchev

read.ip.icl

Read in parameter estimates

## **Description**

From ICL output, read in estimates of item parameters. Invoked automatically when the model is estimated via irroys. If that is not the case, file must be a file produced with the write\_item\_param file command in ICL.

#### Usage

```
read.ip.icl(file)
```

#### **Arguments**

file

File name

#### Value

A list with two elements, est and se, for the parameter estimates and their standard errors, correspondingly. Because ICL does not compute standard errors, se will be NULL. est is a matrix with one row per item, and three columns: [,1] item discrimination a, [,2] item difficulty b, and [,3] asymptote c. For the 1PL and 2PL models, all asymptotes are equal to 0; for the 1PL, the discriminations are all equal but not necessarily equal to 1.

## Author(s)

Ivailo Partchev

read.qu.icl 23

#### **Description**

From ICL output, read in estimates of item parameters. file must be a file produced with the write\_latent\_dist file command in ICL. Quadrature objects are used when estimating abilities with eap and for some of the scaling methods in sca.

## Usage

```
read.qu.icl(file)
```

#### **Arguments**

file File name

#### Value

A list of:

quad.points A vector of quadrature points

quad.weights A vector of the corresponding quadrature weights

## Author(s)

Ivailo Partchev

## See Also

```
normal.qu, eap, sca
```

read.resp

Read responses from a file

## **Description**

Reads responses to a questionnaire from a text file

## Usage

```
read.resp(file, na = ".")
```

## **Arguments**

file File name

na The symbol used to represent missing data

24 sca

#### **Details**

Included for those who are too faint-hearted to write as.matrix(read.table(file, head=F)). Of course, data can be entered into R in many other ways.

The data values in the file must be separated with blanks.

Responses are the empirical data used in IRT. Note that irroys deals with models for dichotomous data, and typically expects data consisting of zeroes and ones, without any missing values (non-responses are considered as wrong responses). In fact, there are only two commands in irroys that accept other kinds of data: sco and tgp.

read.resp does accept missing data and values other than 0 and 1. Use sco and a key to score multiple choice responses to 0/1. If you have dichotomous data that contains NAs, you can use sco without a key to change all NA to 0.

#### Value

A matrix, typically of zeroes and ones, representing the correct or wrong responses given by persons (rows) to items (columns).

#### Author(s)

Ivailo Partchev

## See Also

```
sco, tgp,
```

#### **Examples**

```
## Not run:
    r <- read.resp("c:/myfiles/irt.dat")
## End(Not run)</pre>
```

sca

Linear transformation of the IRT scale

## **Description**

Linearly transform a set of IRT parameters to bring them to the scale of another set of parameters. Four methods are implemented: Mean/Mean, Mean/Sigma, Lord-Stocking, and Haebara.

#### Usage

```
sca(old.ip, new.ip, old.items, new.items, old.qu = NULL,
new.qu = NULL, method = "MS", bec = FALSE)
```

sca 25

## **Arguments**

old.ip	A set of parameters that are already on the desired scale
new.ip	A set of parameters that must be placed on the same scale as old.ip
old.items	A vector of indexes pointing to those items in old. ip that are common to both sets of parameters
new.items	The indexes of the same items in new.ip
old.qu	A quadrature object for old.ip, typically produced by the same program that estimated old.ip. Only needed if method="LS" or method="HB"
new.qu	A quadrature object for new.ip, typically produced by the same program that estimated new.ip. Only needed if $method="HB"$
method	One of "MM" (Mean/Mean), "MS" (Mean/Sigma), "SL" (Stocking-Lord), or "HB" (Haebara). Default is "MS"
bec	Use back-equating correction? When TRUE, the Stocking-Lord or Hebaera procedures will be adjusted for back-equating (see Hebaera, 1980). Ignored when method is MM or MS. Default is FALSE.

#### Value

A list of:

slope The slope of the linear transformation
intercept The intercept of the linear transformation
scaled.ip The parameters in new.ip transformed to a scale that is compatible with old.ip

#### Author(s)

Ivailo Partchev and Tamaki Hattori

#### References

Kolen, M.J. & R.L. Brennan (1995) Test Equating: Methods and Practices. Springer.

Haebara, T. (1980) Equating logistic ability scales by a weighted lest squares method. Japanese Psychological Research, 22, p.144–149

```
## Not run:
# a small simulation to demonstrate transformation to a common scale
# fake 50 2PL items
pa <- cbind(runif(50,.8,2), runif(50,-2.4,2.4), rep(0,50))
# simulate responses with two samples of different ability levels
r.1 <- sim(ip=pa[1:30,], x=rnorm(1000,-.5))
r.2 <- sim(ip=pa[21:50,], x=rnorm(1000,.5))
# estimate item parameters
p.1 <- est(r.1, engine="ltm")
p.2 <- est(r.2, engine="ltm")
# plot difficulties to show difference in scale</pre>
```

26 sco

```
plot(c(-3,3), c(-3,3), ty="n", xlab="True",ylab="Estimated",
    main="Achieving common scale")
text(pa[1:30,2], p.1$est[,2], 1:30)
text(pa[21:50,2], p.2$est[,2], 21:50, co=2)
# scale with the default Mean/Sigma method
pa.sc = sca(old.ip=p.1$est, new.ip=p.2$est, old.items=21:30, new.items=1:10)
# add difficulties of scaled items to plot
text(pa[21:50,2], pa.sc$scaled.ip[,2], 21:50, co=3)
## End(Not run)
```

sco

Score a multiple choice test

#### **Description**

Given a key, score a multiple choice test, i.e. recode the original choices to right (1) or wrong (0). Missing responses are treated as wrong.

## Usage

```
sco(choices, key, na.false = FALSE)
```

#### **Arguments**

choices The original responses to the items in the test: persons as rows, items as columns.

May contain NA.

key A vector containing the key (correct answers) to the items in choices. If not

given, the function will check if all data are either 0, 1, or NA: if yes, NA are

recoded as 0, else an error message is returned.

na.false Recode non-responses to false responses?

#### Value

A matrix of responses scored 0=wrong 1=correct, and possibly NA

#### Author(s)

Ivailo Partchev

```
res <- sco(Unscored, key=c(2,3,1,1,4,1,2,1,2,3,3,4,3,4,2,2,4,3))
```

Scored 27

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SCO	rad

Binary (true/false) responses to a test

## Description

Real-life data set containing the responses to a test, scored as true or false.

#### **Format**

A data set with 472 persons and 18 items.

Scored2p
----------

Example item parameters

## **Description**

Item parameter estimates for the 2PL model, estimated with 1tm from the example data set Scored. These are provided as a check, and to speed up the examples for the various functions in the package.

#### **Format**

A list of two matrices: est contains the parameter estimates, and se contains the standard errors (see also est).

scp

Plot observed and predicted scores against ability

## **Description**

Produces a plot of IRT true scores (test response function at the estimated ability) with a confidence band (plus/minus standard error). The observed sum scores are shown in red.

## Usage

```
scp(resp, ip, theta = NULL)
```

#### **Arguments**

resp	A matrix of binary responses to a test, with persons as rows and items as columns.
ip	Item parameters: a matrix with one row per item, and three columns: [,1] item discrimination $a$ , [,2] item difficulty $b$ , and [,3] asymptote $c$ .
theta	An object containing ability estimates, as output by function mlebme or eap. If NULL, MLE will be estimated from resp and ip.

28 sim

## Value

None

#### Author(s)

Ivailo Partchev

#### See Also

```
mlebme, eap, tsc, trf
```

## **Examples**

```
scp(Scored, Scored2pl$est)
```

sim

Simulate response data

## Description

Simulate responses from the 1PL, 2PL, or 3PL model

## Usage

```
sim(ip, x = NULL)
```

## **Arguments**

ip Item parameters: a matrix with one row per item, and three columns: [,1] item

discrimination a, [,2] item difficulty b, and [,3] asymptote c.

x A vector of values of the latent variable ("abilities").

#### Value

A matrix of responses: persons as rows, items as columns, entries are either 0 or 1, no missing data

## Author(s)

Ivailo Partchev

```
pa <- cbind(runif(20,.8,2), runif(20,-2.4,2.4), rep(0,50)) rs <- sim(ip=pa, x=rnorm(1000))
```

tet 29

tet

Approximate tetrachoric correlation matrix

## **Description**

Matrix of tetrachoric correlations using the approximation by Bonett and Price (2005).

## Usage

tet(d)

## **Arguments**

d

a matrix (or data frame, which will be converted to a matrix) containing only zeroes an ones. NAs are not allowed.

#### Value

A matrix of approximate tetrachoric correlations.

## Author(s)

Ivailo Partchev

#### References

Douglas G. Bonett and Robert M. Price (2005). Inferential Methods for the Tetrachoric Correlation Coefficient. Journal of Educational and Behavioral Statistics, Vol. 30, No. 2, pp. 213–225

## **Examples**

```
tetras <- tet(Scored)</pre>
```

tgp

Non-parametric option curves

## **Description**

A plotting function producing non-parametric analogues of the IRF for each option in a multiple choice item not unlike those in Jim Ramsay's TestGraf program.

## Usage

```
tgp(choices, key, item,
  main = "Non-parametric response function", co = 1,
  label = FALSE)
```

30 tia

## **Arguments**

choices	A matrix of responses to multiple-choice items: persons as rows, items as columns. As a rare exception in irtoys, responses must not be recoded to 0/1, and there may be missing responses.
key	A vector containing the key (correct answers) to the items in choices.
item	A single number pointing to the item (column of choices) to plot.
main	The main title of the plot, given that add=F.
СО	The colour of the curves. Default is 1 for black. Use co=NA to plot each curve in a different colour.
label	When label=T, individual curves will be labeled with the item number.

## Author(s)

Ivailo Partchev

#### References

James O. Ramsay (2000). TestGraf: A program for the graphical analysis of multiple choice test and questionnaire data. McGill University, Montreal, Canada

## See Also

```
qrs, irf, plot.irf
```

## **Examples**

```
\label{eq:condition} $$ key=c(2,3,1,1,4,1,2,1,2,3,3,4,3,4,2,2,4,3) $$ tgp(choices=Unscored, key=key, item=4, co=NA, label=TRUE) $$
```

tia

Elementary test-item analysis

## Description

Elementary analysis of the items in a test and the test sumscores based on Classical Test Theory.

## Usage

```
tia(choices, key, ...)
```

## **Arguments**

choices	The original responses to the items in the test: persons as rows, items as columns. May contain NA.
key	A vector containing the key (correct answers) to the items in choices. If not given, the function will check if all data are either 0, 1, or NA: if yes, NA are recoded as 0, else an error message is returned.
	Other parameters that may be passed to sco or cov

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#### Value

A list with three elements:

**testlevel** A list of statistics at test level (currently, only Cronbach's alpha, may be extended in future)

**itemlevel** A matrix showing, for each item, the proportion of correct responses, the correlation with the sum score, and the alpha that the test would have if the item were dropped.

**optionlevel** A matrix showing, for each possible choice in the multiple-choice item, the proportion of responses given, and the correlation with the sum score for the test (including the item). The correct response is highlighted with asterisks.

#### Author(s)

Ivailo Partchev

#### **Examples**

```
itemsum \leftarrow tia(Unscored, key=c(2,3,1,1,4,1,2,1,2,3,3,4,3,4,2,2,4,3))
```

tif

Test information function

## Description

Returns the test information function (TIF) of the 3PL (1PL, 2PL) model. The TIF is the sum of the item information functions (IIF) in a test, and indicates the precision of measurement that can be achieved with the test at any value of the latent variable, bein inversely related to measurement variance.

## Usage

```
tif(ip, x = NULL)
```

## **Arguments**

Х

ip	Item parameters: a matrix with one row per item, and three columns: [,1] item
	discrimination $a$ , [,2] item difficulty $b$ , and [,3] asymptote $c$ .

The values of the latent variable ( $\theta$  in the equation above), at which the TIF will be evaluated. If not given, 99 values spaced evenly between -4 and +4 will be used, handy for plotting.

## **Details**

A common use of this function would be to obtain a plot of the TIF.

32 trf

## Value

A list of:

x A copy of the argument x

f A vector containing the TIF values

#### Author(s)

Ivailo Partchev

#### See Also

```
plot.tif, iif
```

#### **Examples**

```
plot(trf(Scored2pl$est))
```

trf

Test response function

## **Description**

Returns the test response function (TRF) of the 3PL (1PL, 2PL) model. The TRF is the sum of the item response functions (IRF) in a test, and represents the expected score as a function of the latent variable  $\theta$ .

## Usage

```
trf(ip, x = NULL)
```

#### **Arguments**

ip Item parameters: a matrix with one row per item, and three columns: [,1] item

discrimination a, [,2] item difficulty b, and [,3] asymptote c.

x The values of the latent variable ( $\theta$  in the equation above), at which the IRF will

be evaluated. If not given, 99 values spaced evenly between -4 and +4 will be

used, handy for plotting.

## **Details**

A common use of this function would be to obtain a plot of the TRF.

#### Value

A list of:

x A copy of the argument x

f A vector containing the TRF values

tsc 33

#### Author(s)

Ivailo Partchev

#### See Also

```
plot.trf, irf
```

## **Examples**

```
plot(trf(Scored2pl$est))
```

tsc

True scores with standard errors

## Description

Computes the IRT true scores (test response function at the estimated ability) and an estimate of their standard error via the delta theorem, treating item parameters as known).

## Usage

```
tsc(ip, theta)
```

## Arguments

ip Item parameters: a matrix with one row per item, and three columns: [,1] item

discrimination a, [,2] item difficulty b, and [,3] asymptote c.

theta An object containing ability estimates, as output by function mlebme or eap

#### Value

A matrix with the true scores in column 1, and their standard errors of measurement (SEM) in column 2

## Author(s)

Ivailo Partchev

## See Also

```
mlebme, eap, trf
```

```
th <- mlebme(resp=Scored, ip=Scored2pl$est)
tsc(Scored2pl$est, th)</pre>
```

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Unscored Original, unscored multiple-choice responses to a test
Unscored Original, unscored multiple-choice responses to a test

#### **Description**

Real-life data set containing the responses to a test, before they have been recoded as true or false. Can be used with only two functions in the package: sco and npp. All other functions expect binary data, which can be produced with sco.

#### **Format**

A data set with 472 persons and 18 items. Each item has 4 possible answers, of which only one is true. There are many NA, which can be treated as wrong responses.

wle

Bias-corrected (Warm's) estimates of ability

## Description

Weighted likelihood estimates (WLE) of ability, designed to remove the first order bias term from the ML estimates. WLE are finite for response patterns consisting of either uniformly wrong or uniformly correct responses.

#### Usage

```
wle(resp, ip)
```

## Arguments

resp	A matrix of responses: persons as rows, items as columns, entries are either 0 or 1, no missing data
ip	Item parameters: a matrix with one row per item, and three columns: [,1] item discrimination $a$ , [,2] item difficulty $b$ , and [,3] asymptote $c$ .

## Value

A matrix with the ability estimates in column 1, and their standard errors of measurement (SEM) in column 2, and the number of non-missing reponses in column 3

#### Author(s)

Ivailo Partchev

#### References

Warm T.A. (1989) Weighted Likelihood Estimation of Ability in Item Response Theory. Psychometrika, 54, 427-450.

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## See Also

mlebme, eap

```
th.bce <- wle(resp=Scored, ip=Scored2pl$est)</pre>
```

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